

$$F_T = F_g/2 \quad a = 0$$

$$F_{\text{net}} = 2 F_T - F_g = ma$$

$$2 \left(1.1 \times \frac{F_g}{2} \right) - F_g = ma$$

$$1.1 \cancel{m}g - \cancel{m}g = \cancel{m}a$$

$$\boxed{a = 0.1g}$$

Circular Motion (not on the test Oct 26th)

Demonstration:

Swing the bucket over my head and the water doesn't fall out.

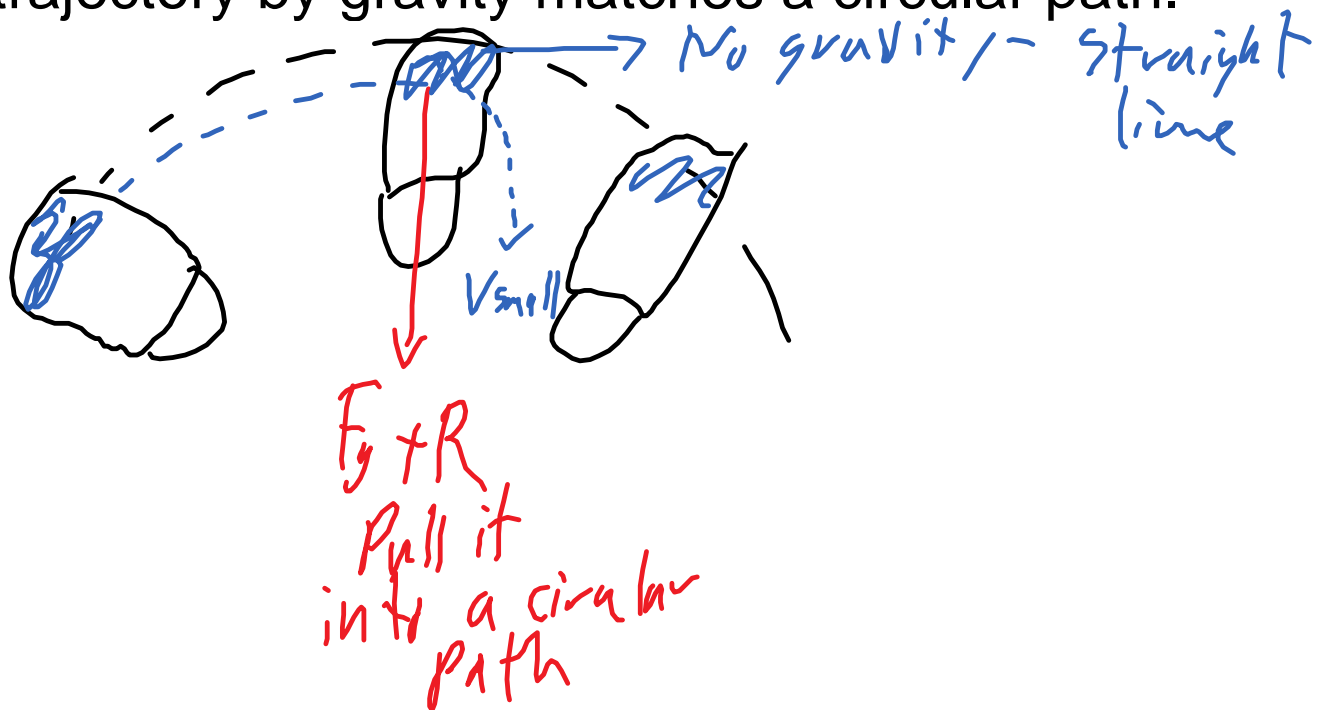
What's the deal?

2 minutes write a guestimate/explanation

Aswin - the inertia of the water tends to keep it moving in a straight line.

gravity accelerates the water down

If it is moving fast enough, the deflection of the trajectory by gravity matches a circular path.



Let's derive:

Look at a mass m , moving at speed, v , in uniform circular motion (constant speed).

Not constant velocity - the direction is constantly changing.

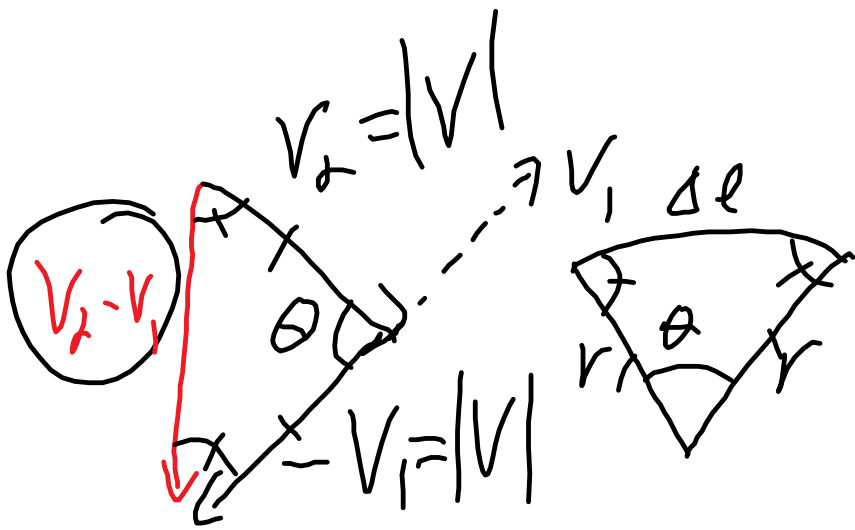
$$arc\ length = \Delta l$$

arc length = Δx
 radius of
 circular path = r



$$a = \frac{\Delta V}{\Delta t} = \frac{V_2 - V_1}{\Delta t}$$

Vector



Kinda like similar triangles,
 ratio of sides $\frac{V_2 - V_1}{V} = \frac{\Delta l}{r}$

$$a = \frac{V_2 - V_1}{\Delta t} = \frac{\Delta l V}{r \Delta t}$$

$$\frac{\Delta l}{\Delta t} = V$$

valid for

$$a = \frac{v^2}{r}$$

valid for
uniform
circular motion

What if the circular motion is not uniform?

The same but instead of being the acceleration, it is the centripetal component of the acceleration a_c (towards the centre of the circle).

The tangential component of the acceleration, a_t , give the change in speed.

$$a_c = v^2/r$$

For uniform circular motion, there is no tangential acceleration, the only acceleration is centripetal.

So $F_{\text{net}} = ma = ma_c = mv^2/r$ for uniform circular motion.

for non-uniform circular motion,

F_c is the centripetal force, the component of the net force towards the centre of the circle.

circle.

$$F_c = mv^2/r$$

eg. A skateboarder, mass 80.0 kg wants to do a loop in a big tube. If his centre of mass moves through a circular path of radius 2.0m,

a) what is the minimum speed at the top to make the loop?

$$a = g$$

$$v^2/r = g$$

$$v = \sqrt{gr}$$

$$v = \sqrt{9.81 \times 2} = 4.42944691807002$$

$$v = 4.4 \text{ m/s}$$

a) If there is no energy lost to friction, what is his speed at the bottom?

top = bottom

gravitational and kinetic energy = E_k

$$2 \cancel{m}gh + 1/2 \cancel{m}v_{\text{top}}^2 = 1/2 \cancel{m}v_{\text{bottom}}^2$$

$$v = \sqrt{(2 \times 9.81 \times 4) + (4.4294 \times 4.4294)} = 9.904523429221621$$

$$9.9 \text{ m/s}$$

a) What is his acceleration at the bottom?

$$a = v^2/r = (9.90 \times 9.90)/2 = 49.005 = 49 \text{ m/s}^2$$

(rather big)

a) what is the normal force on his feet
(apprx) at the bottom?

$$F_{\text{net}} = R - F_g$$

$$R = F_{\text{net}} + F_g$$

$$= 80\text{kg} \times 49\text{m/s}^2 + 80\text{kg} \times 9.81\text{m/s}^2$$

$$= 80 \times (49 + 9.81) = 4,704.8$$

4.7 kN wow! that's a lot!

he doesn't go a full 2m and he bends his
knees to minimize this

study for the test:

SHM, vectors, projectiles, Dynamics
(ch11, ch 3, ch 4)